

Code:MSM5004

Lectures : 2 Tutorials : 2 Practical : 0 Credits : 3

Code:MSM5005

Lectures : 2 Tutorials : 2 Practical : 0 Credits : 3  
 Representation of solutions by other methods: separation of variables; similarity of solutions; transform methods (Fourier, Laplace); converting nonlinear PDE into ODE (Hopf Cole transform, potential functions, Legendre and Hodograph transforms); Asymptotics (singular perturbations, Laplace's method, geometric optics, stationary phase, homogenization); Power series (non characteristic surfaces, real analytic functions, Cauchy - Kovalevskaya theorem).

## References

1. L. C. Evans, Partial Differential Equations (Part I only), Graduate Studies in mathematics, Vol. 19, AMS, 1996.
2. F. John, Partial Differential Equations, Springer Science and Business, 1982.
3. T. Amarnath, An Elementary Introduction to Partial Differential Equations, Alpha Science International, 2003.
4. P. Prasad and R. Ravindran, Partial Differential Equations, New Age International, 1985.
5. I. N. Sneddon, Elements of Partial Differential Equations, Dover Publications, 2006. Advanced

## Topology

1. Fundamental groups and homotopy theory: homotopic mappings, contractible spaces, essential and inessential maps, homotopically equivalent spaces. Fundamental group of space, examples, homotopy groups  $\pi_n(X)$   $n \geq 1$ . Munkres, Topology, Chapter-8; Hocking & Young: Topology, Chapter-4.
2. Simplicial Theory: Simplicial complexes, barycentric subdivision, simplicial maps, approximation theorem, fundamental group of a simplicial complex. Hocking & Young: Topology, Chapter-5.
3. Covering Space Theory: Covering Spaces, examples, properties of covering spaces, relation between fundamental group of covering space and its base and tower correspondence, universal covering space construction: treatment as in - W. Massey: Introduction to Algebraic Topology.
4. Simplicial and Singular homology theory (a) Oriented complexes, chains, cycles and boundary operator Homology groups and Betti numbers and torsion coefficients zero dimensional homology, Euler Poincaré formula, simplicial maps and induced homeomorphisms, chain complexes and chain maps and induced homeomorphisms. Cone complexes Hocking & Young: Topology, Chapter-6 (b) Singular homology theory, exact sequences, excision, Mayer-Vietoris sequence etc. treatment as in Greenberg: Lectures on Algebraic Topology (Benjamin) Hocking & Young: Topology, Chapter-7 (c) Čech Homology Theory Axiomatic homology theory of Eilenberg, Steenrod and its properties; Čech homology and properties Hocking & Young: Topology, Chapter-8.

## References

1. Maunder C.F., Algebraic Topology, Dover Publications, 1996.

## Algebraic Geometry

Varieties: Affine and projective varieties, coordinate rings, morphisms and rational maps, local ring of a point, function fields, dimension of a variety. Curves:

Singular points and tangent lines, multiplicities and local rings, intersection multiplicities, Bezout's theorem for plane curves, Max Noether's theorem and some of its applications, group law on a nonsingular cubic, rational parametrization, branches and valuations. 12

Code:MSM5006

Lectures : 2 Tutorials : 2 Practical : 0 Credits : 3

Code:MSM5007

Lectures : 2 Tutorials : 2 Practical : 0 Credits : 3  
References

1. S.S. Abhyankar, Algebraic Geometry for Scientists and Engineers, American Mathematical Society, 1990.
2. W. Fulton, Algebraic Curves, Benjamin, 1969.
3. J. Harris, Algebraic Geometry: A First Course, Springer-Verlag, 1992.
4. M. Reid, Undergraduate Algebraic Geometry, Cambridge University Press, Cambridge, 1990.
5. I.R. Shafarevich, Basic Algebraic Geometry, Springer-Verlag, Berlin, 1974.
6. R.J. Walker, Algebraic Curves, Springer-Verlag, Berlin, 1950.

Analytic Number Theory

Arithmetic functions - Combinatorial study of  $\phi(n)$ ,