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## ON THE DIMENSION OF VERTEX LABELING OF k-UNIFORM DCSL OF k-UNIFORM CATERPILLAR

A distance compatible set labeling (dcsl) of a connected graph G is an injective set assignment  $f:V(G)\to 2^X$ , X being a nonempty ground set, such that the corresponding induced function  $f^\oplus:E(G)\to 2^X\setminus\{\varnothing\}$  given by  $f^\oplus(uv)=f(u)\oplus f(v)$  satisfies  $|f^\oplus(uv)|=k_{(u,v)}^fd_G(u,v)$  for every pair of distinct vertices  $u,v\in V(G)$ , where  $d_G(u,v)$  denotes the path distance between u and v and  $k_{(u,v)}^f$  is a constant, not necessarily an integer. A dcsl f of G is k-uniform if all the constant of proportionality with respect to f are equal to k, and if G admits such a dcsl then G is called a k-uniform dcsl graph. The k-uniform dcsl index of a graph G, denoted by  $\delta_k(G)$  is the minimum of the cardinalities of X, as X varies over all k-uniform dcsl-sets of G. A linear extension E of a partial order E of E is a linear order on the elements of E, such that E is the minimum number of linear extensions on E whose intersection is ' $\Xi$ '. In this paper we prove that dim $(F) \subseteq \delta_k(P_n^{+k})$ , where E is the range of a E-uniform dcsl of the E-uniform caterpillar, denoted by E-uniform E-uniform dcsl of the E-uniform caterpillar, denoted by E-uniform E-uniform E-uniform dcsl of the E-uniform caterpillar, denoted by E-uniform E-uniform E-uniform dcsl of the E-uniform caterpillar, denoted by E-uniform E-uniform E-uniform dcsl of the E-uniform caterpillar, denoted by E-uniform E-uniform E-uniform dcsl of the E-uniform caterpillar, denoted by E-uniform E-uniform E-uniform E-uniform dcsl of the E-uniform caterpillar, denoted by E-uniform E-uniform E-uniform E-unifor

Key words and phrases: k-uniform dcsl index, dimension of a poset, lattice.

## INTRODUCTION

Acharya [1] introduced the notion of vertex *set-valuation* as a set-analogue of number valuation. For a graph G = (V, E) and a nonempty set X, Acharya defined a *set-valuation* of G as an injective *set-valued* function  $f: V(G) \to 2^X$ , and defined a *set-indexer*  $f^{\oplus}: E(G) \to 2^X \setminus \{\emptyset\}$  as a *set-valuation* such that the function given by  $f^{\oplus}(uv) = f(u) \oplus f(v)$  for every  $uv \in E(G)$  is also injective, where  $2^X$  is the set of all subsets of X and  $'\oplus'$  is the binary operation of taking the symmetric difference of subsets of X.

Acharya and Germina [2], introduced the particular kind of set-valuation for which a metric, especially the cardinality of the symmetric difference, associated with each pair of vertices is k (where k be a constant) times that of the distance between them in the graph [2]. In other words, determine those graphs G = (V, E) that admit an injective set-valued function  $f: V(G) \to 2^X$ , where  $2^X$  is the power set of a nonempty set X, such that, for each pair of distinct vertices u and v in G, the cardinality of the symmetric difference  $f(u) \oplus f(v)$  is k times

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